

Tantia University, Sri Ganganagar

Syllabus for Ph.D. Entrance exam

Subject- Mathematics

Maximum Marks-100

Part A- 50 (Research Methodology)

Part B- 50 (Subject Wise)

PART-A

Research Methodology and Statistics

- UNIT 1: Meaning of Research
 Aims, nature and scope of research
 Prerequisites of research
- UNIT 2: Research Problem
 Meaning of research problem Sources of research problem Characteristics of a
 good research problem
 Hypothesis: Meaning and types of hypothesis. Research proposal or synopsis.
- UNIT 3: Types and Methods of Research
 Classification of Research
 Pure and Applied Research
 Exploring or Formulative Research
 Descriptive Research
 Diagnostic Research/Study
 Evaluation Research/Studies
 Action Research
 Experimental Research
 Historical Research
 Surveys
 Case Study
 Field Studies
- Unit 4: Review of Related Literature
 Purpose of the review. Identification of the related literature. Organizing the
 related literature.
- UNIT 5: Data Collection (Sampling) Sampling and Population Techniques of sampling
 Selection Characteristics of a good sample Types of data.
- UNIT 6: Tools of Data Collection
 Observation, Interview, Questionnaire, Rating scales, Attitude scales, Schedules,
 Characteristics of good research tools.
- UNIT 7: Statistics
 Concept of statistics, relevance in education, parametric and non-parametric
 data; graphical representation of data: histogram, frequency polygon, ogive and
 pie chart; Measures of Central Tendency: concept, computation and

interpretation; measures of variability: concept, computation and interpretation; normal probability curve: concept, application and interpretation.

Correlation: concept, computation and interpretation- Product Moment, Rank Order, Biserial, Point Biserial, Phi, Contingency, Tetrachoric; significance of mean: concept, computation and interpretation of significance of t-test(correlated and uncorrelated, matched, paired-unpaired, matching- paired); ANOVA(One way) :concept, computation and interpretation, regression and prediction; chi square: concept, computation and interpretation (equal and normal probability).

UNIT 8: Research Report

Format of the research report Style of writing the report References and bibliography

Reference books:

1. Best John W. and James Kahn, V., 1989, Research in Education, Sixth Edition, Prentice-Hall of India Pvt.Ltd, New Delhi.
2. Sharma R.A., 1992, Fundamentals of Educational Research, Loyal Book Depot, Meerut, UP, India.
3. Kulbir Singh Sidhu, 1990, Methodology of Research in Education, Sterling Publishers Pvt. Ltd., New Delhi.
4. Lokesh Koul, 1997 Methodology of educational Research, third edition, Vikas Publishing House Pvt. Ltd. , New Delhi.
5. Kothari C.R., 1990, Research Methodology Methods and Techniques, Wiley Eastern Limited, New Delhi.
6. Borg Walter R., Gall Meridith D., 1983, Educational Research an Introduction, Fourth Edition, Longaman, New York & London.
7. Nitko Anthony J., 1983, Educational Tests and Measurement an Introduction, Harcourt Brace Jovanovich, Inc., New York.
8. Aggarwal Y.P., 1988, Statistical Methods Sterling Publishers Pvt. Ltd., New Delhi.
9. Garret Hnery E., 1985 Statistics in Psychology and Education, Viakils, Feffer and Simon, Bombay.
10. Guilford, J.P., and Benjamin Fruchter, 1982 Fundamentals of statistics in Psychology and Education, Fifth edition, Mc Graw-Hill Book Company, New York.
11. Gupta S.C. and Kapoor V.K., 1999, Fundamentals of Mathematical Statistics, Sultan Chand& Sons Educational Publishers, New Delhi.
12. Grewal P.S., Methods of Statistics Analysis, Sterling Publishers Pvt. Ltd., New Delhi.
13. Bruce W. Tuckman, Statistics in Psychology and Education.

Part-B

Mathematics

Unit I: Analysis

Convergence of sequence and series, Bolzano Weierstrass theorem, Heine Borel theorem, Uniform convergence of sequence and series, Riemann Integral, Improper Integral.

Countability of sets, Lebesgue measure on the real line, length of intervals, open and closed sets on real line. Outer and inner Lebesgue measure, Lebesgue measurable sets, properties of measurable sets, Borel sets and their measurability, non-measurable sets, Cantor's Ternary sets and their properties.

Measurable functions, characteristic function, step function, continuous function, set of measure zero, Borel measurable function, the structure of measurable function.

Riemann integral and its deficiency, Lebesgue integral of bounded function, comparison of Riemann and Lebesgue integrals, properties of Lebesgue integral for bounded measurable function. Lebesgue integral for unbounded functions. General Lebesgue integral, improper integral.

Uniform convergence almost everywhere, convergence in measure, Reisz's theorem, Egoroff's theorem, Fatou's lemma, Monotone convergence theorem.

Unit 2: Linear Algebra

Linear transformation, rank and nullity of a linear transformation, Sylvester's law of nullity, subspaces, quotient spaces, Schauder basis.

Algebra of linear transformations, orthogonal and supplementary linear transformations, dual space, linear functional, bidual, canonical isomorphism.

Matrix of a linear transformation, change of basis, equivalent and similar matrices, minimal polynomials, invertible linear transformation.

Eigenvalues, eigenvectors, maximal polynomials, diagonal vectors of a square matrix, Jordan block, Jordan canonical form, Jordan normal form. Quadratic forms, reduction and classification of quadratic forms.

Trace and transpose of a linear transformation, adjoint, Hermitian adjoint. Unitary and normal linear operators.

Unit 3: Mechanics

Moments of inertia, kinetic energy, angular momentum, mechanics of a particle and system of particles, kinematics of a rigid body, Euler's angles, Euler's dynamical equations, two dimensional motion of a rigid body, compound pendulum, constraints.

D'Alembert's principle, Lagrange's equations of motion, techniques of calculus of variations. Hamilton's principles, Hamilton's equations of motion, contact transformation, Lagrange's and Poisson brackets, integral in variances, Hamilton-Jacobi Poisson equations.

Unit 4: Topology

Definition and examples of metric spaces, open and closed spheres, open and closed sets, convergence, completeness, Cantor's intersection theorem, dense sets and separable spaces, Baire's category theorem, continuous mappings, uniform continuity.

Definition and examples of topological spaces, neighbourhood system of a point, limit points, closed sets, closure, interior and boundary, bases and sub-bases, continuity, homeomorphism, subspaces and product spaces. Local base, first and second countable spaces. Separable spaces, Lindelof's theorem.

Compactness, finite intersection property, Heine Borel theorem, locally compact spaces, sequential compactness, Bolzano Weierstrass property, Lebesgue covering lemma, total boundedness.

Separation Axioms, T_i ($i = 0,1,2,3,4$) spaces, regular and completely regular spaces. Normal and completely normal spaces.

Connected spaces, components, locally connected spaces. Totally connected spaces, totally disconnected spaces, pathwise connectivity.

Unit 5: Differential Geometry

Covariant, contravariant and mixed tensors, Riemannian metric tensor, Christoffel symbols, covariant derivatives of higher rank tensor, differentiable curves in E^3 , tangent vector, principal normal, binormal, curvature and torsion, Serret-Frenet formulas, fundamental theorem for space curve. Vector fields, covariant differentiations, connexion forms and structural equations in E^3 .

Surfaces in E^3 , first fundamental forms, geodesic on surface, second fundamental forms, tensor derivative, Gauss-Weingarten formulae, integrability condition, Gauss & Mainardi Codazzi equations, Meusnier theorem, geodesic curvature, line of curvature, asymptotic lines, Gauss and mean curvature, minimal surfaces, third fundamental forms.

Unit 6: Ordinary Differential Equations

Existence & uniqueness theorem of solution of initial value problems for second and higher order differential equations.

Series solution of second order linear differential equations near ordinary point, singularity and the solution in the neighbourhood of regular singular point, Euler equation and Frobenius method

Linear homogeneous boundary value problems, variation of parameters. Eigenvalues and Eigenfunctions, Sturm-Liouville boundary value problems

Unit 7: Partial Differential Equations

Lagrange's and Charpit's general method for solving PDE's, Cauchy problem for first order PDE's

Classification of second order PDE's, general solution of higher order PDE's with constant coefficients, method of separation of variables for Laplace, heat and wave equations.

Unit 8: Abstract Algebra

Congruences, Euler's function, primitive roots. Groups, subgroups, normal subgroups, quotient groups, homomorphisms. Cyclic groups, permutation groups, Cayley's theorem, class equations, Sylow theorems.

Rings, ideals, prime and maximal ideals, quotient rings, unique factorization domain, principal ideal domain, Euclidean domain, polynomial rings and irreducibility criteria.

Unit 9: Functional Analysis

Definition and examples of normed and Banach spaces, incomplete normed spaces, completion, subspaces, quotient spaces, Schauder basis.

Definition and examples of bounded linear operator, relation between continuity and boundedness, null space, spaces of bounded linear operators, equivalent norms, open mapping theorem, closed graph theorem, uniform boundedness principle.

Definition and examples bounded linear functional, relation between continuity and boundedness, dual spaces, duals of \mathbb{R}^n , \mathbb{C}^n , $\ell^p(n)$ ($1 < p < \infty$), c_0 , ℓ^1 and ℓ^p ($1 < p < \infty$), Hahn Banach theorem, embedding and reflexivity, adjoint operator. Weak and weak* convergence.

Inner product spaces and Hilbert spaces, Schwartz inequality, parallelogram equality, subspaces, completion. Orthogonality of vectors, orthogonal complement and projection theorem. Orthogonal sets and Fourier analysis, complete orthogonal sets.

Unit 10: Complex Analysis

Representation of complex numbers, analytic function, Cauchy Riemann equations, power series. Some elementary functions, Harmonic functions.

Properties of line integral, zeros of an analytic function, Cauchy's theorem, Cauchy's integral formula, Cauchy's inequality. Fundamental theorem of algebra, Poisson's formula, Liouville's theorem, Rouché's theorem, argument principle.

Residues and poles, classification of isolated singularities, Taylor's and Laurent's series. Winding numbers and Cauchy Residue theorem.

Application of residue theorem in evaluation of improper real integrals and evaluation of sum.

Conformal mapping properties, Schwarz Lemma, Riemann mapping theorem, Maximum modulus theorem, Analytical continuation.